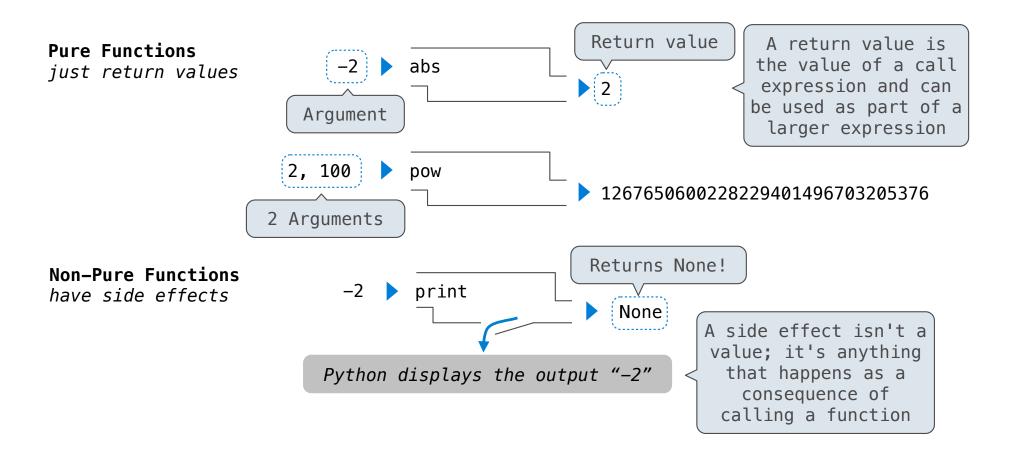


Pure Functions & Non-Pure Functions



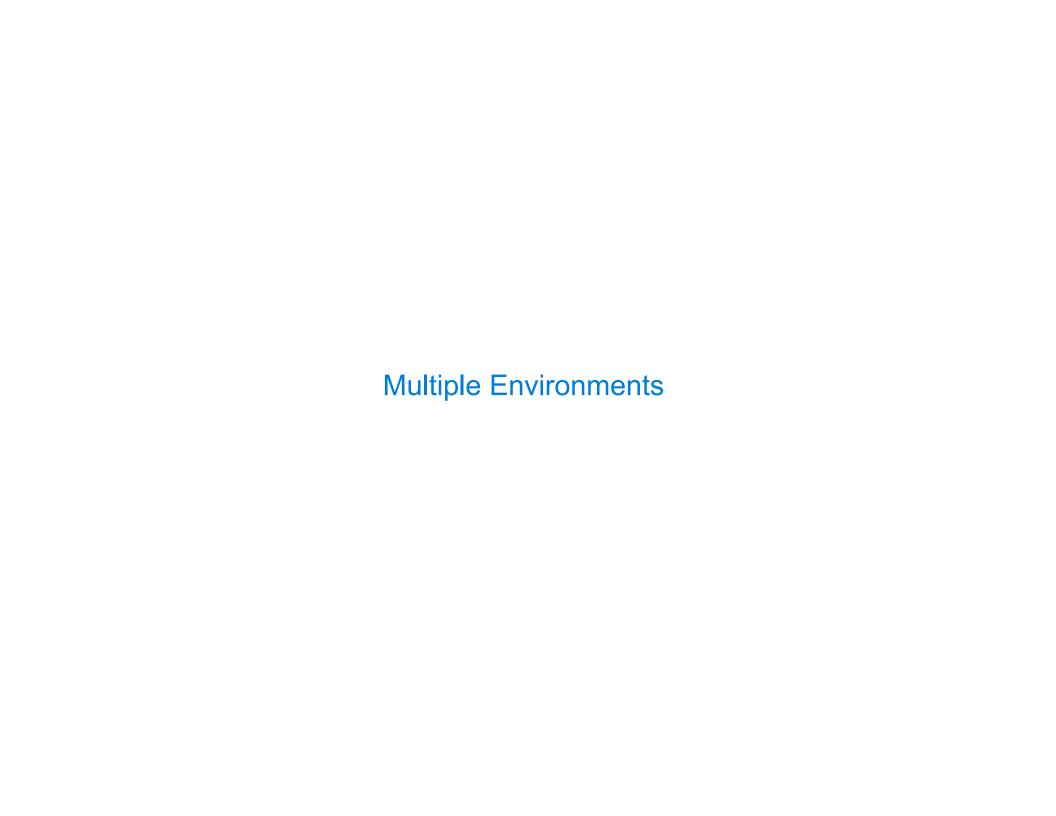
Example: Print Then Return

Implement a function h(x) that first prints, then returns, the value of f(x).

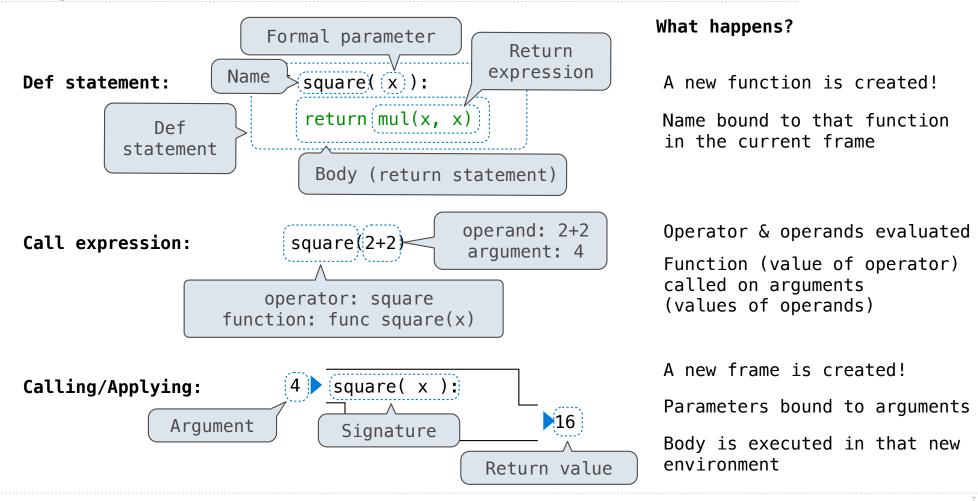
```
\begin{array}{lll} \text{def } h(x) \colon & \text{def } h(x) \colon & \text{def } h(x) \colon \\ & \text{return print}(f(x)) & \text{print}(f(x)) & \text{y = } f(x) \\ & \text{return } f(x) & \text{print}(y) \\ & & \text{return y} \end{array}
```

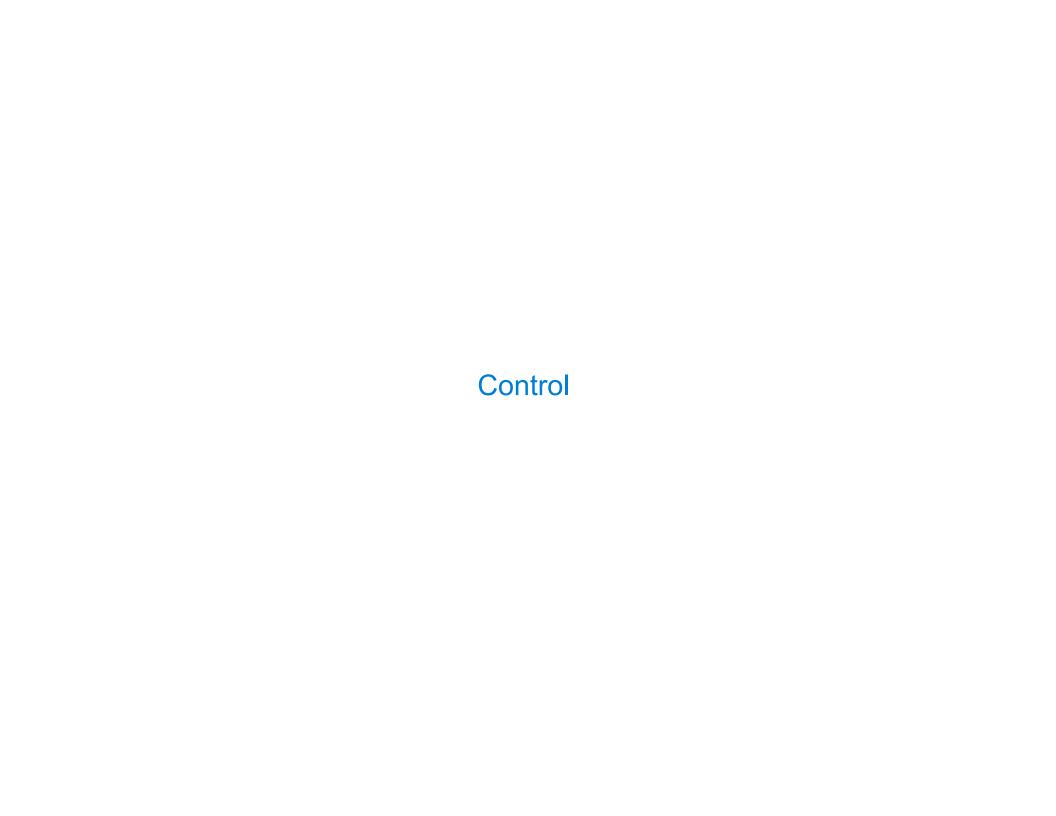
What's a function f for which implementations (B) and (C) would have different behavior?

(Demo)



Life Cycle of a User-Defined Function





Conditional Statements

Conditional statements (often called "If" Statements) contain statements that may or may not be evaluated.

		x=10	x=1	x=-1
<pre>if x > 2: print('big') if x > 0: print('positive')</pre>	Two separate (unrelated) conditional statements	big positive	positive	
<pre>if x > 2: print('big') elif x > 0: print('positive')</pre>	One statement with two clauses: if and elif Only one body can ever be executed	big	positive	
<pre>if x > 2: print('big') elif x > 0: print('positive') else: print('not pos')</pre>	One statement with three clauses: if, elif, else Only one body can ever be executed	big	positive	not pos

While Statements

While statements contain statements that are repeated as long as some condition is true.

Important considerations:

- How many separate names are needed and what do they mean?
- The while condition **must eventually become a false value** for the statement to end (unless there is a return statement inside the while body).
- Once the while condition is evaluated, the entire body is executed.

```
Names and their initial values

i, total = 0, 0

The while condition is evaluated before each iteration

A name that appears in the while condition is changing

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1

i = i + 1
```

Example: Nice Numbers

Nice Numbers

Rounding off 2,799 to 2,800 makes it nice.

Definition: A nice number doesn't have 98 or 99 or 01 or 02 among its digits.

Not-so-nice numbers: 99 2,799 5,016 9,902 1,200,456 98,402,001

Nicer versions: 100 2,800 5,000 10,000 1,200,000 100,000,000

These numbers are nice enough already and unaffected: 755 2,859 45,622,895

Implement nice, which takes a positive integer n. It returns the nearest nice number to n.

- For numbers that end in 98 or 99 or 01 or 02, round to the nearest 100.
- · Look for 98 or 99 or 01 or 02 among the digits that aren't at the end.

To solve a problem, describe a process and work through an example:

4	7	9	8	4	0	2	0	0	1
4	7	9	8	4	0	2	0	0	0
4	7	9	8	4	0	0	0	0	0
4	8	0	0	0	0	0	0	0	0

(Demo)

Example: Prime Factorization

Prime Factorization

Each positive integer n has a set of prime factors: primes whose product is n

```
8 = 2 * 2 * 2

9 = 3 * 3

10 = 2 * 5

11 = 11

12 = 2 * 2 * 3
```

One approach: Find the smallest prime factor of n, then divide by it

$$858 = 2 * 429 = 2 * 3 * 143 = 2 * 3 * 11 * 13$$

(Demo)