

# Generators

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## Announcements

# Tree Practice

## Spring 2023 Midterm 2 Question 4(a)

Implement `exclude`, which takes a tree `t` and a value `x`. It returns a tree containing the root node of `t` as well as each non-root node of `t` with a label not equal to `x`. The parent of a node in the result is its nearest ancestor node that is not excluded.

```
def exclude(t, x):
    """Return a tree with the non-root nodes of tree t labeled anything but x.
```

```
>>> t = tree(1, [tree(2, [tree(2), tree(3), tree(4)]), tree(5, [tree(1)])])
```

```
>>> exclude(t, 2)
```

```
[1, [3], [4], [5, [1]]]
```

```
>>> exclude(t, 1) # The root node cannot be excluded
```

```
[1, [2, [2], [3], [4]], [5]]
```

```
"""
```

```
    filtered_branches = map(lambda y: exclude(y, x), branches(t))
```

```
    bs = []
```

```
    for b in filtered_branches:
```

```
        if label(b) == x:
```

37% of students got this right

In Spring 2023, 20% of students got this right

```
            bs.extend(branches(b))
```

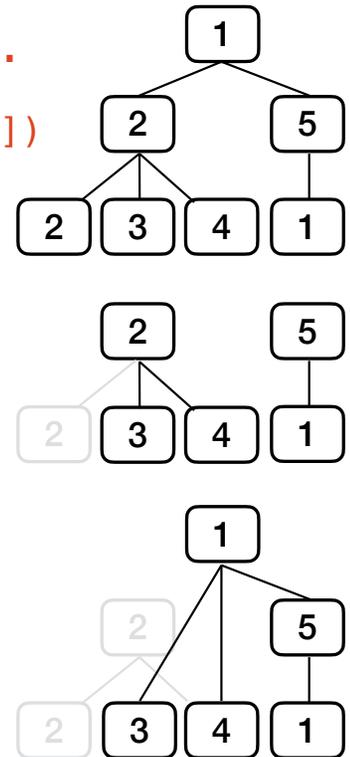
24% got it right

```
        else:
```

```
            bs.append(b)
```

```
    return tree(label(t), bs)
```

30% got it right; 1 of 4 options



## Min Practice

## Match the description to the code

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`w = {...}` # a dict with unique keys and values

`m = {v: k for k, v in w.items()}`

Which expression evaluates to?

1. The key that has the smallest value in `w`
2. The value that has the smallest key in `w`
3. The smallest absolute difference between a key and its value

`min(w.keys(), key=lambda k: w[k])`

`min(w.keys(), key=lambda k: m[k])`

`min(w.values(), key=lambda v: w[v])`

`min(w.values(), key=lambda v: m[v])`

`min(w.keys(), key=lambda k: abs(k - w[k]))`

`min(w.keys(), key=lambda k: abs(k - m[k]))`

`min(map(lambda k: abs(k - w[k]), w.keys()))`

`min(map(lambda k: abs(k - m[k]), w.keys()))`

# Generators

## Generators and Generator Functions

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```
>>> def plus_minus(x):
...     yield x
...     yield -x

>>> t = plus_minus(3)
>>> next(t)
3
>>> next(t)
-3
>>> t
<generator object plus_minus ...>
```

A *generator function* is a function that **yields** values instead of **returning** them

A normal function **returns** once; a *generator function* can **yield** multiple times

A *generator* is an iterator created automatically by calling a *generator function*

When a *generator function* is called, it returns a *generator* that iterates over its yields

(Demo)

## Spring 2023 Midterm 2 Question 5(b)

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**Definition.** When parking vehicles in a row, a motorcycle takes up 1 parking spot and a car takes up 2 adjacent parking spots. A string of length  $n$  can represent  $n$  adjacent parking spots using % for a motorcycle, <> for a car, and . for an empty spot.

For example: `'.%%.<><>'` (Thanks to the Berkeley Math Circle for introducing this question.)

Implement `park`, a generator function that yields all the ways, represented as strings, that vehicles can be parked in  $n$  adjacent parking spots for positive integer  $n$ .

```
def park(n):
    """Yield the ways to park cars and motorcycles in n adjacent spots.

    >>> sorted(park(1))
    ['%', '.']
    >>> sorted(park(2))
    ['%%', '%.', '.%', '..', '<>']
    >>> len(list(park(4))) # some examples: '<><>', '.%%.', '%<>%', '%.<>'
    29
    """
```

## Example: Call Expressions

## Problem Definition

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### From Discussion 0:

Imagine you can call only the following three functions:

- $f(x)$ : Subtracts one from an integer  $x$
- $g(x)$ : Doubles an integer  $x$
- $h(x, y)$ : Concatenates the digits of two different positive integers  $x$  and  $y$ . For example,  $h(789, 12)$  evaluates to 78912 and  $h(12, 789)$  evaluates to 12789.

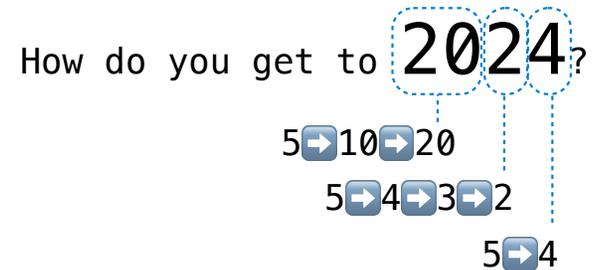
**Definition:** A *small expression* is a call expression that contains only  $f$ ,  $g$ ,  $h$ , the number 5, and parentheses. All of these can be repeated. For example,  $h(g(5), f(f(5)))$  is a small expression that evaluates to 103.

What's the shortest *small expression* you can find that evaluates to 2023?

### A Simple Restatement:

You start with 5. You can:

- Subtract 1 from a number
- Double a number
- Glue two numbers together



(Demo)

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## A Computational Approach

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```
def f(x):                def g(x):                def h(x, y):
    return x - 1          return 2 * x          return int(str(x) + str(y))

def smalls(n):
    """Yield all call expressions involving f, g, h, and 5 that have n calls.

    >>> [exp for exp in smalls(7) if eval(exp) == 2024]
    ['g(h(g(5), g(g(f(f(5))))))']
    """
    if n == 0:
        yield '5'
    else:
        for operand in smalls(n-1):
            yield 'f(' + operand + ')'
            yield 'g(' + operand + ')'
        for k in range(n):
            for first in smalls(k):
                for second in smalls(n-k-1):
                    if eval(first) > 0 and eval(second) > 0:
                        yield 'h(' + first + ', ' + second + ')'
```